## After the exam of 08.09.2015: Typical errors, comments etc.

Question 1
Error: the hint is used but not proved.
Penalty: 25 points.
Comment: the volume of the set $E_{a}=\left\{(x, y, z): x^{2}+y^{4}+z^{6} \leq a\right\}$ is proportional to $a^{11 / 12}$, since the linear transformation $T_{a}:(x, y, z) \mapsto$ $\left(a^{1 / 2} x, a^{1 / 4} y, a^{1 / 6} z\right)$ satisfies $T_{a}\left(E_{1}\right)=E_{a}$ and $\operatorname{det} T_{a}=a^{11 / 12}$.

Alternatively, you may obtain $E_{a}$ from a ball by a nonlinear transformation, and use spherical coordinates (on the ball), but this way is longer.

## Question 2

Error: the square root (of the Gram determinant) is forgotten.
Penalty: 7 points.

## Question 3

Error: the surface of a sphere is proportional to $r^{n}$ (rather than $r^{n-1}$ ). Penalty: 7 points.
Error: the unit normal vector (to a sphere) is $x$ (rather than $\frac{x}{|x|}$ ).
Penalty: 7 points.

## Grades statistics

| Total | Question 1 | Question 2 | Question 3 | Question 4 |
| ---: | ---: | ---: | ---: | ---: |
| 100 |  | 35 | 35 | 30 |
| 98 | 35 | 35 | 28 |  |
| 91 | 28 | 35 | 28 |  |
| 86 |  | 35 | 28 | 23 |
| 75 |  | 35 | 10 | 30 |
| 73 | 10 | 35 | 28 |  |
| 65 | 10 | 35 |  | 20 |
| 63 |  | 35 | 28 |  |
| 60 |  | 35 | 10 | 15 |
|  |  |  |  |  |
| 50 | 0 | 35 |  | 15 |
| 45 | 0 | 35 | 10 |  |
| 45 |  | 18 | 10 | 17 |
| 33 | 0 | 18 | 15 |  |
| 28 | 0 | 28 | 0 |  |
| 18 | 0 | 18 | 0 |  |

